



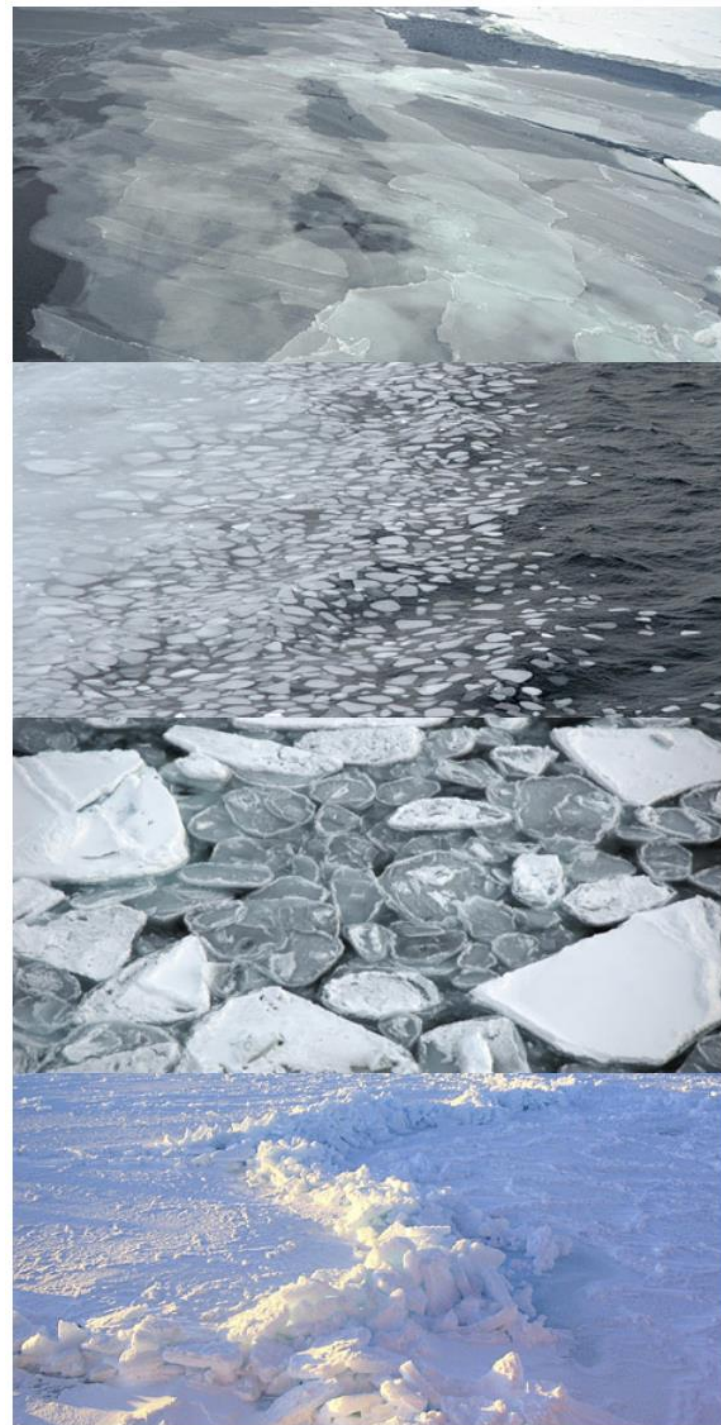
**Jet Propulsion Laboratory**  
California Institute of Technology

# **Ocean state estimation in the under-ice environment**

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Paul Chamberlin (SIO)

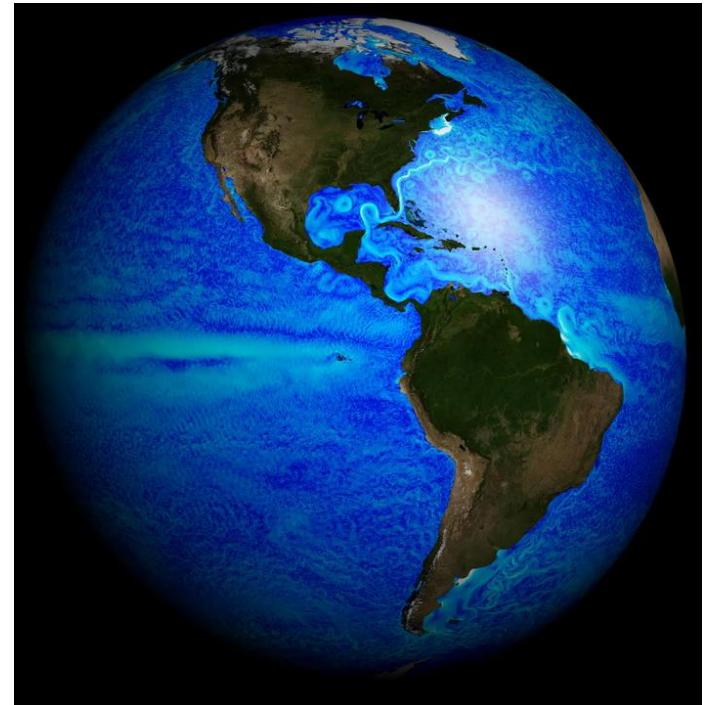


# Ocean state estimation in the under-ice environment

- What is ocean state estimation?
- What have we learned so far about data assimilation in the under-ice environment?
- What has been the impact from *in situ ocean hydrographic* observations under ice?
- What are the most important remaining gaps?

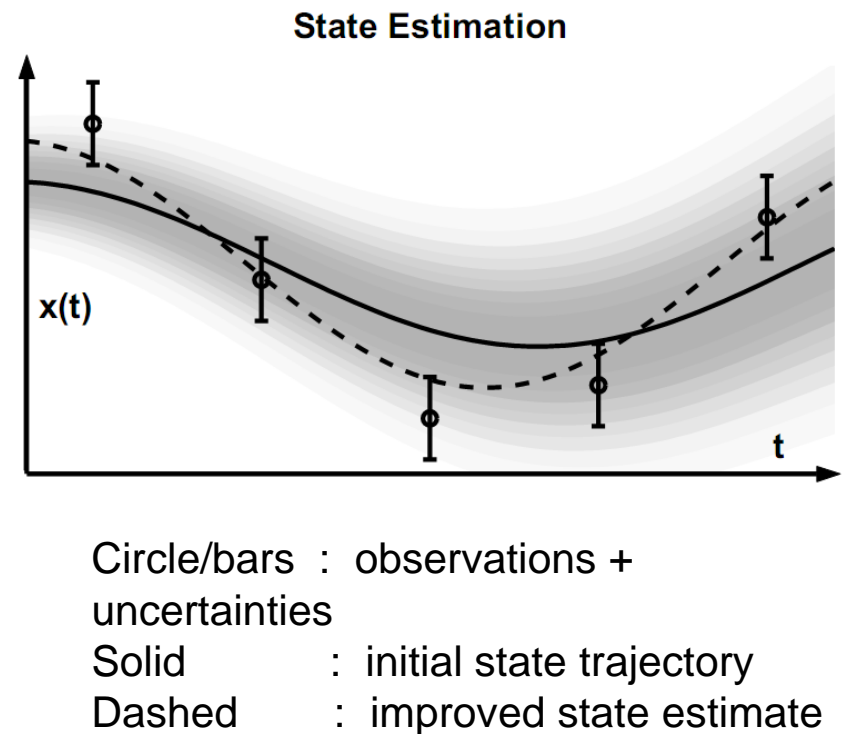
# Four-Dimensional Model Assimilation of Data

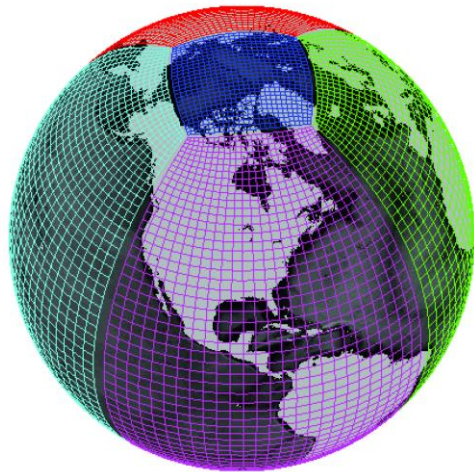
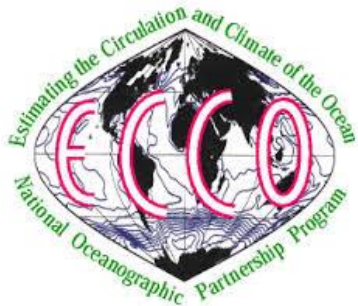
- Four-dimensional (space and time) model assimilation of geophysical data is a method to synthesize **diverse, temporally** and **spatially heterogeneous** observations into a **coherent representation** of an **evolving geophysical system**. The resulting model-data synthesis is referred to as a *state estimate*.
- It is a **systematic, quantitative, and objective means of inference and testing** aimed at advancing understanding and prediction of nonlinear dynamical geophysical systems **where interactions occur continually among relevant physical, chemical, and biogeochemical processes**.



# Ocean State Estimation with the Adjoint Method

- Goal: reconstruct the three-dimensional time-varying ocean-sea ice system (*ocean-ice state estimate*) with a numerical model constrained by observations.
- Minimize the distance in phase space between a model system trajectory and the observations over some time interval.
- The model system trajectory is brought into a state of consistency with the data in a *least-squares sense* using the adjoint of the numerical model.
- The adjoint provides information about how to correct the model system trajectory via adjustments to first-guess model *initial conditions, atmospheric boundary conditions, and other control parameters*.





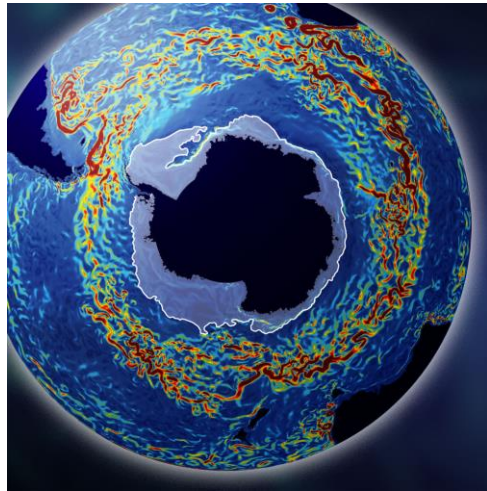
**1992-2015  
Global  
1-degree**

# ECCO: Estimating the Circulation and Climate of the Ocean, Version 4

Variable	Observations
Sea surface height	TOPEX/Poseidon (1993-2005), Jason-1 (2002-2008), Jason-2 (2008-2015), Geosat-Follow-On (2001-2007), CryoSat-2 (2011-2015), ERS-1/2 (1992-2001), ENVISAT (2002-2012), SARAL/AltiKa (2013-2015)
<i>in situ</i> temperature	Argo floats (1995-2015), XBTs (1992-2008), CTDs (1992-2011), <b>Southern Elephant seals as Oceanographic Samplers (SEaOS; 2004-2010)</b> , <b>Ice-Tethered Profilers (ITP, 2004-2011)</b> and other high-latitude CTDs and moorings
<i>in situ</i> salinity	Argo floats (1997-2015), CTDs (1992-2011), <b>SEaOS (2004-2010)</b> , and other new high-latitude CTDs and moorings
Sea surface temperature	AVHRR (1992-2013), AMSR-E (2002-2010)
Sea surface salinity	Aquarius (2011-2013)
Sea-ice concentration	<b>SSM/I DMSP-F11 (1992-2000) and -F13 (1995-2009) and SSMIS DMSP-F17 (2006-2015)</b>
Ocean bottom pressure	GRACE (2002-2014), JPL MASCON Solution

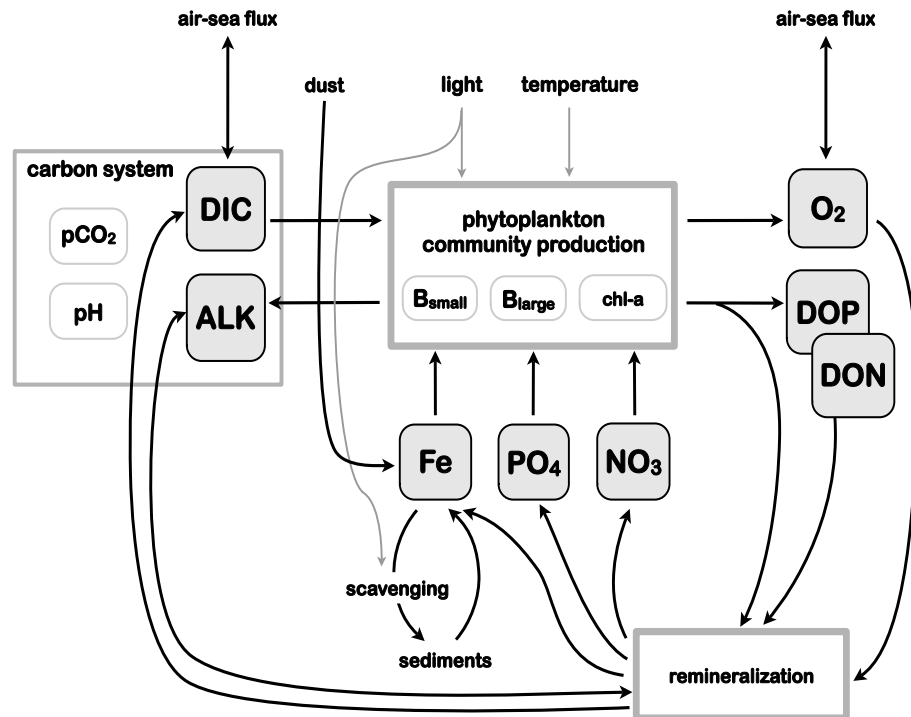


# Biogeochemical-Southern Ocean State Estimate: B-OSE (Mazloff and Verde, SIO)

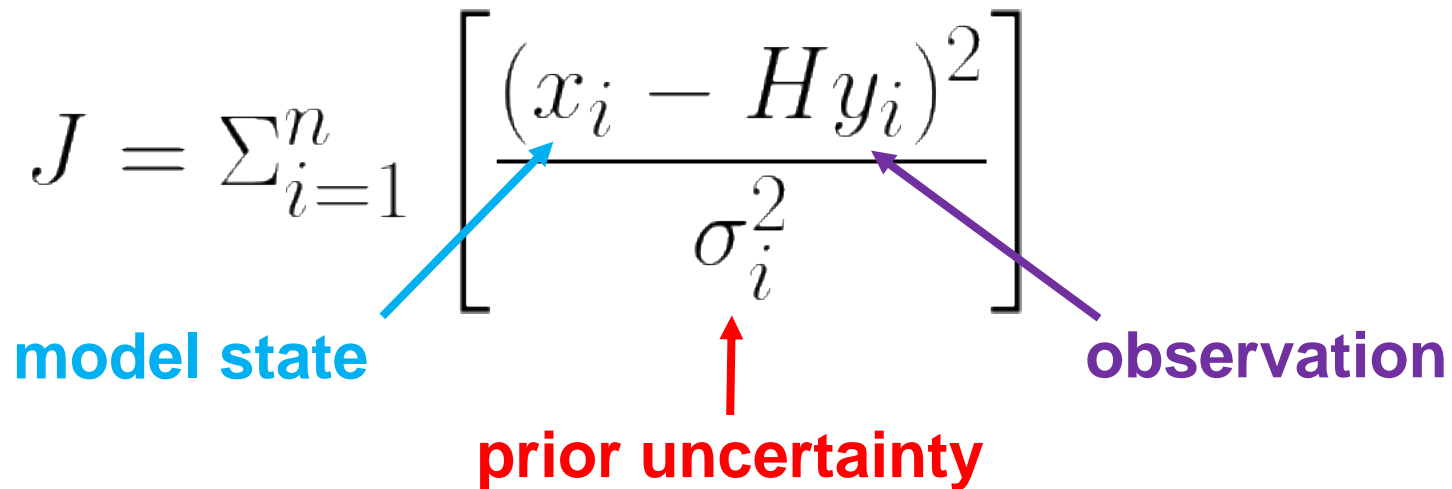


**2008–2012  
Southern Ocean  
1/3-degree**

Variable	Observations
pH	Bio-geochemical Argo
NO <sub>3</sub>	Bio-geochemical Argo
O <sub>2</sub>	Bio-geochemical Argo



# The specification of prior uncertainties is a critical component of ocean state estimation

$$J = \sum_{i=1}^n \left[ \frac{(x_i - Hy_i)^2}{\sigma_i^2} \right]$$


The diagram shows the cost function  $J$  as a sum over  $n$  observations. Each term in the sum is a fraction where the numerator is the squared difference between the model state  $x_i$  and the observation  $Hy_i$ , and the denominator is the prior uncertainty  $\sigma_i^2$ . A blue arrow points from the label "model state" to  $x_i$ , a purple arrow points from the label "observation" to  $y_i$ , and a red arrow points from the label "prior uncertainty" to  $\sigma_i^2$ .

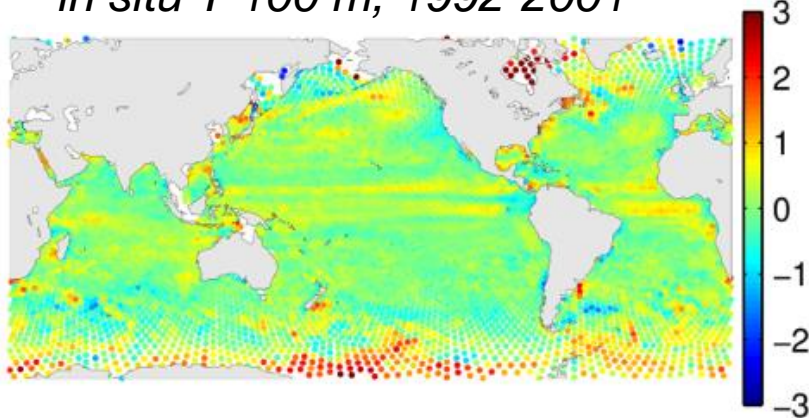
A prior uncertainty is assigned to each observation. Typically, the prior uncertainty is a measure of how well we expect our model to be able to reproduce the observation: the **expected variance** of the **squared model-data residuals**.

*Importantly, these prior uncertainties also determine the criteria for determining whether a state estimate is consistent with the data.*

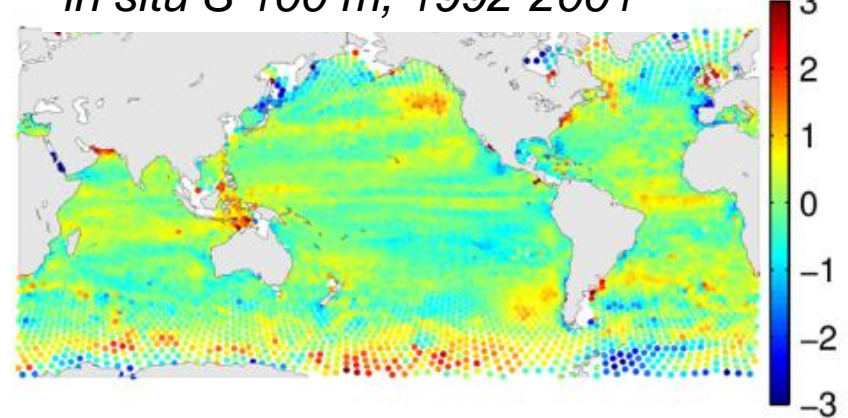
# Consistency of the ECCO ocean-ice state estimate with respect to *in situ* *T* and *S* data

Uncertainty-normalized model-data difference =  $\frac{x_i - Hy_i}{\sigma_i}$

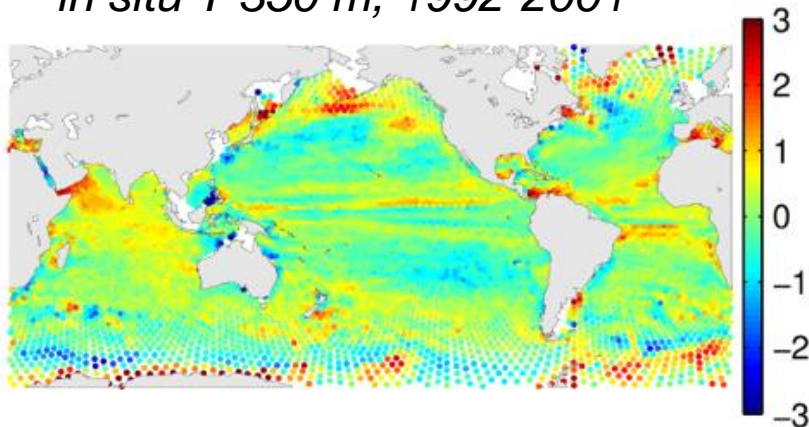
*in situ* *T* 100 m, 1992-2001



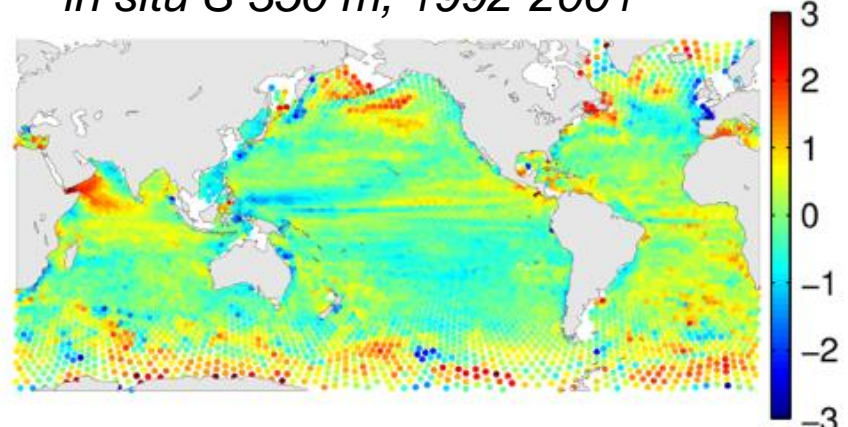
*in situ* *S* 100 m, 1992-2001



*in situ* *T* 350 m, 1992-2001

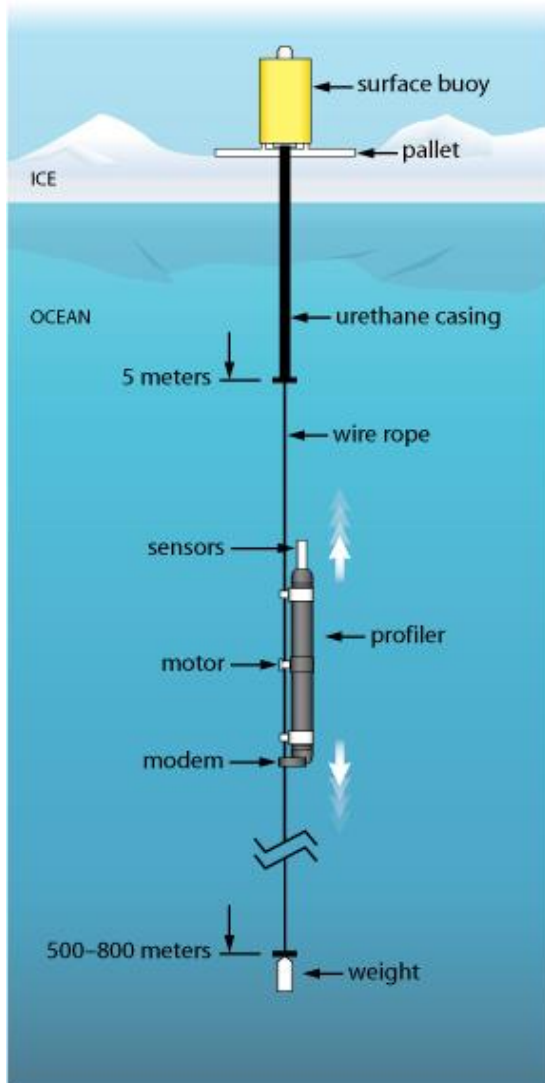


*in situ* *S* 350 m, 1992-2001





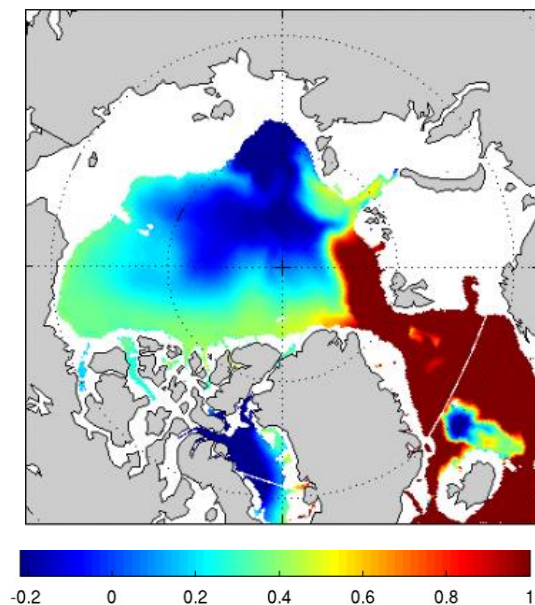
# What has been the impact from *in situ* ocean observations under ice?



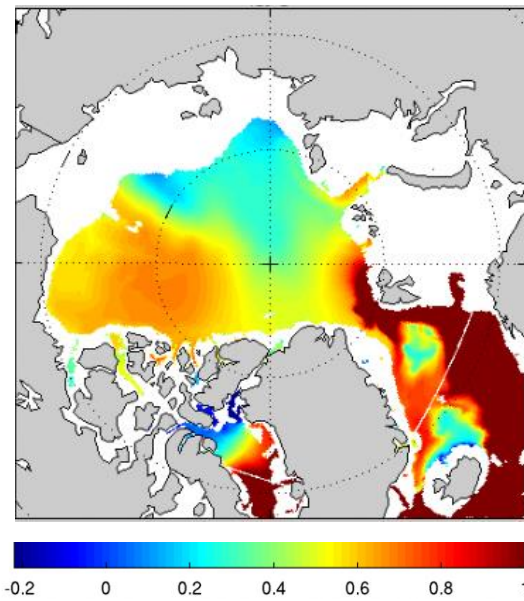
Credit: John Toole/WHOI

# What has been the impact from *in situ* ocean observations under ice?

Ocean T at 220 m, Dec 2012

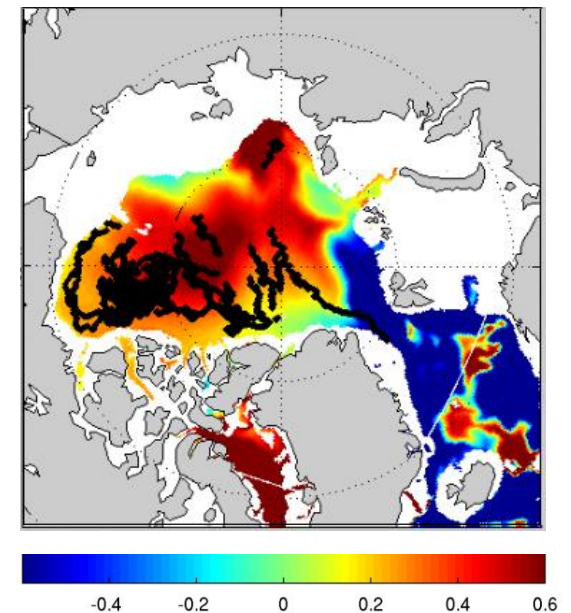


Pre ITP data  
synthesis



Post ITP data  
synthesis

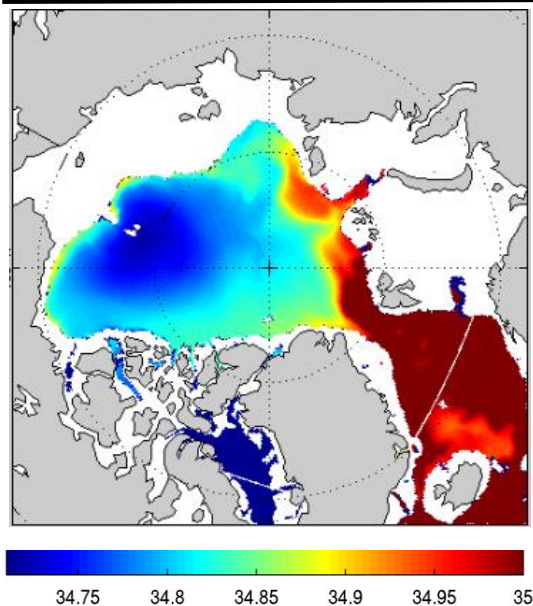
T Difference



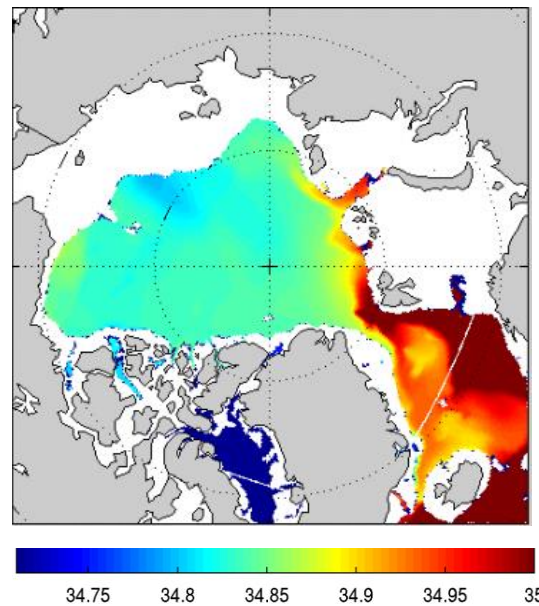
Post – Pre ITP data  
synthesis

# What has been the impact from *in situ* ocean observations under ice?

Ocean S at 220 m, Dec 2012

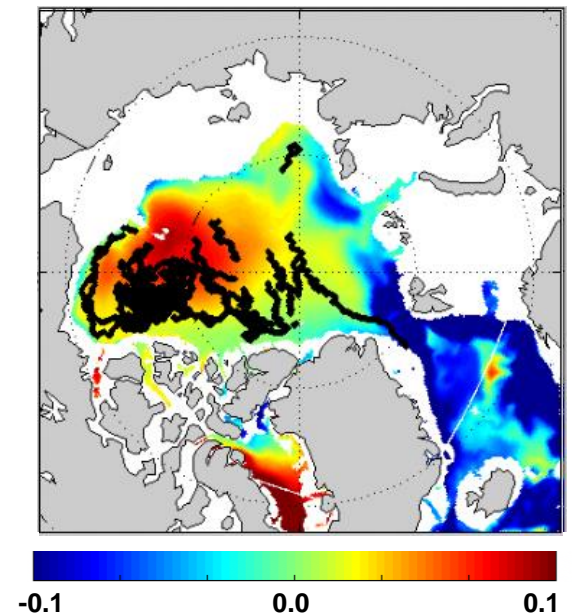


Pre ITP data  
synthesis



Post ITP data  
synthesis

S Difference



Post – Pre ITP data  
synthesis

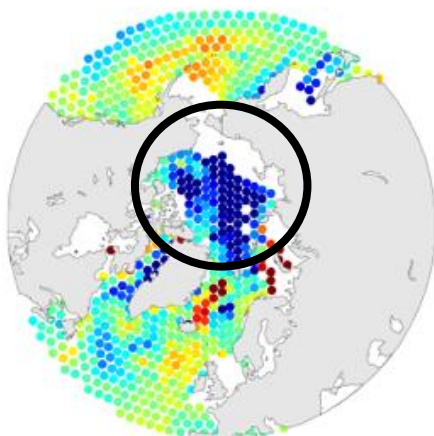


# What has been the impact from in situ ocean observations under ice?

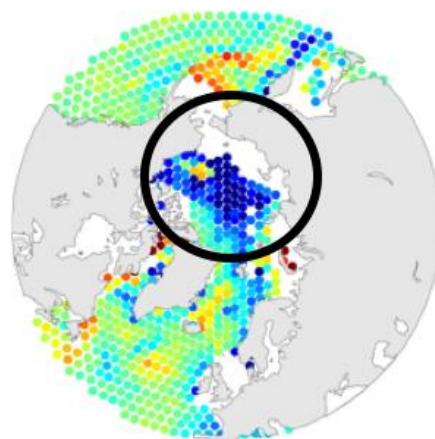
Uncertainty normalized model-data in situ T and S differences before and after ITP data constraints

pre-ITP

T 350m (1992 to 2011)

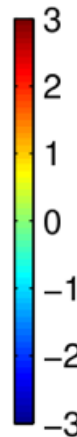
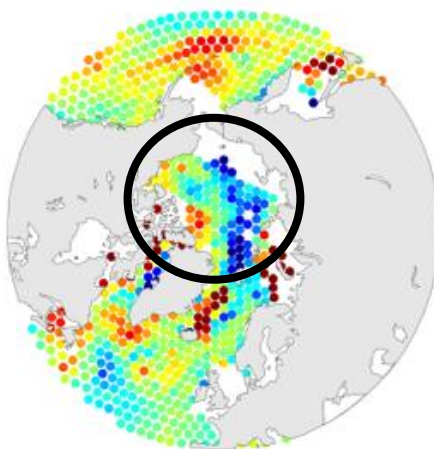


S 350m (1992 to 2011)

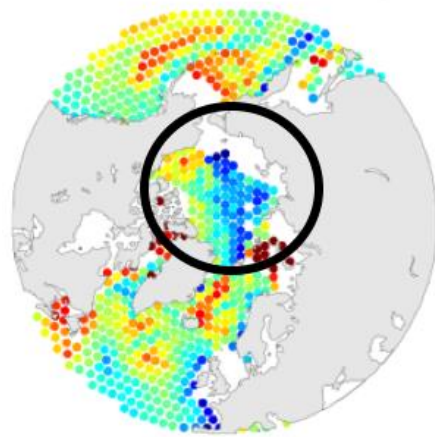


Post-ITP

T 350m (1992 to 2011)



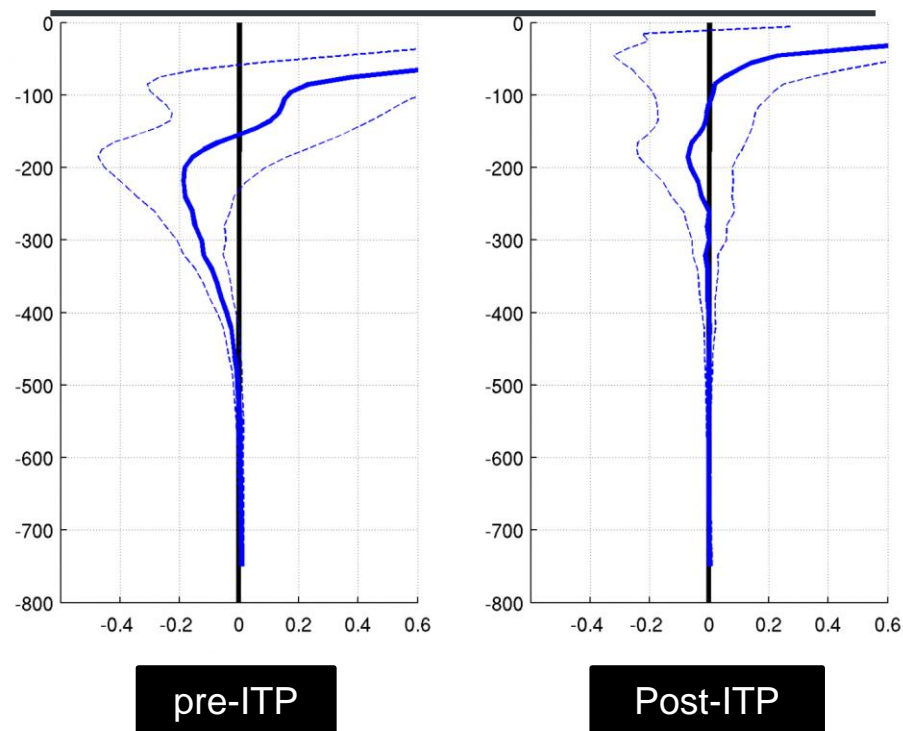
S 350m (1992 to 2011)



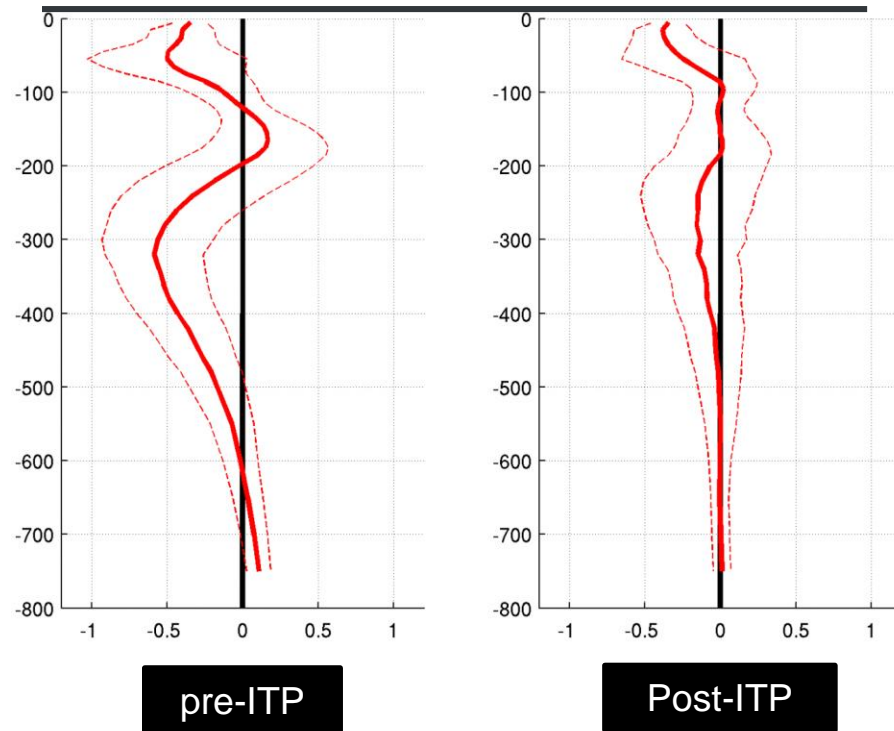
# What has been the impact from in situ ocean observations under ice?

Distribution of model-data T and S differences before and after ITP data synthesis

*Salinity*



*Temperature*

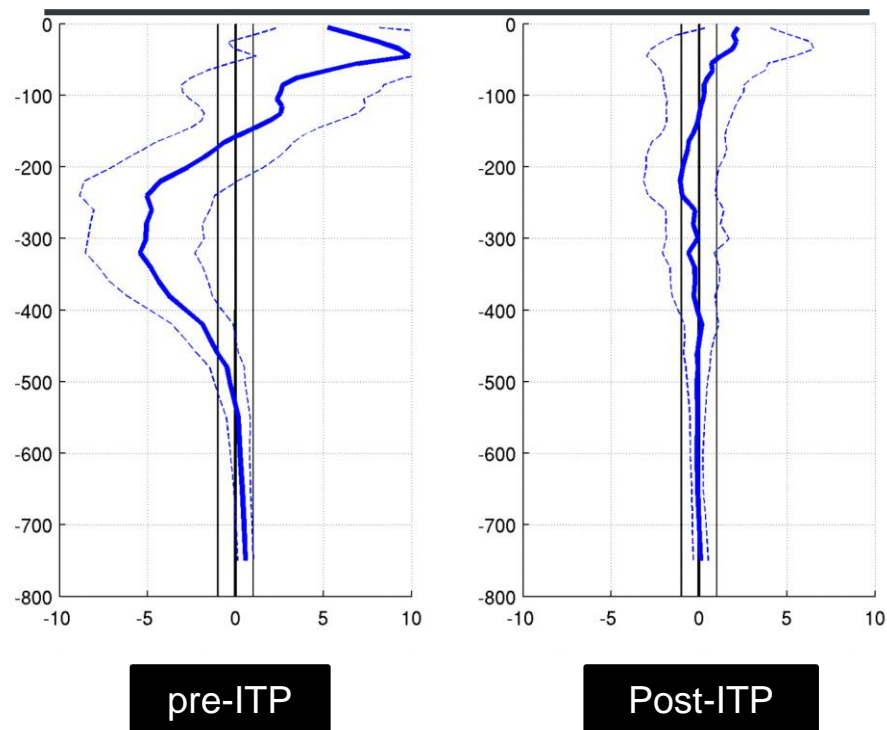




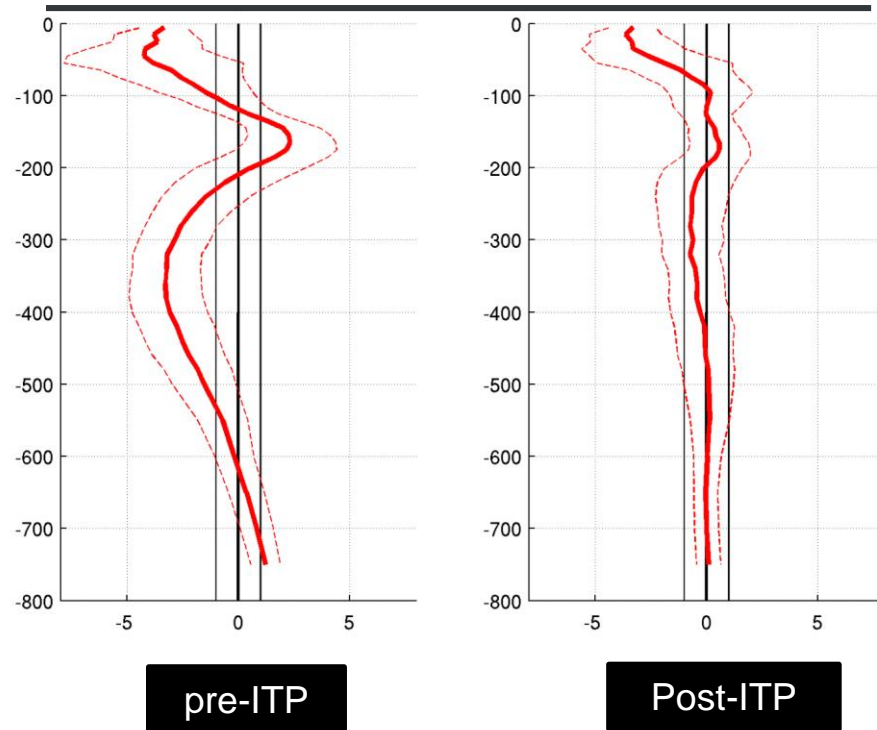
# What has been the impact from in situ ocean observations under ice?

Distribution of uncertainty-normalized model-data T and S differences before and after ITP data synthesis

*Salinity*



*Temperature*

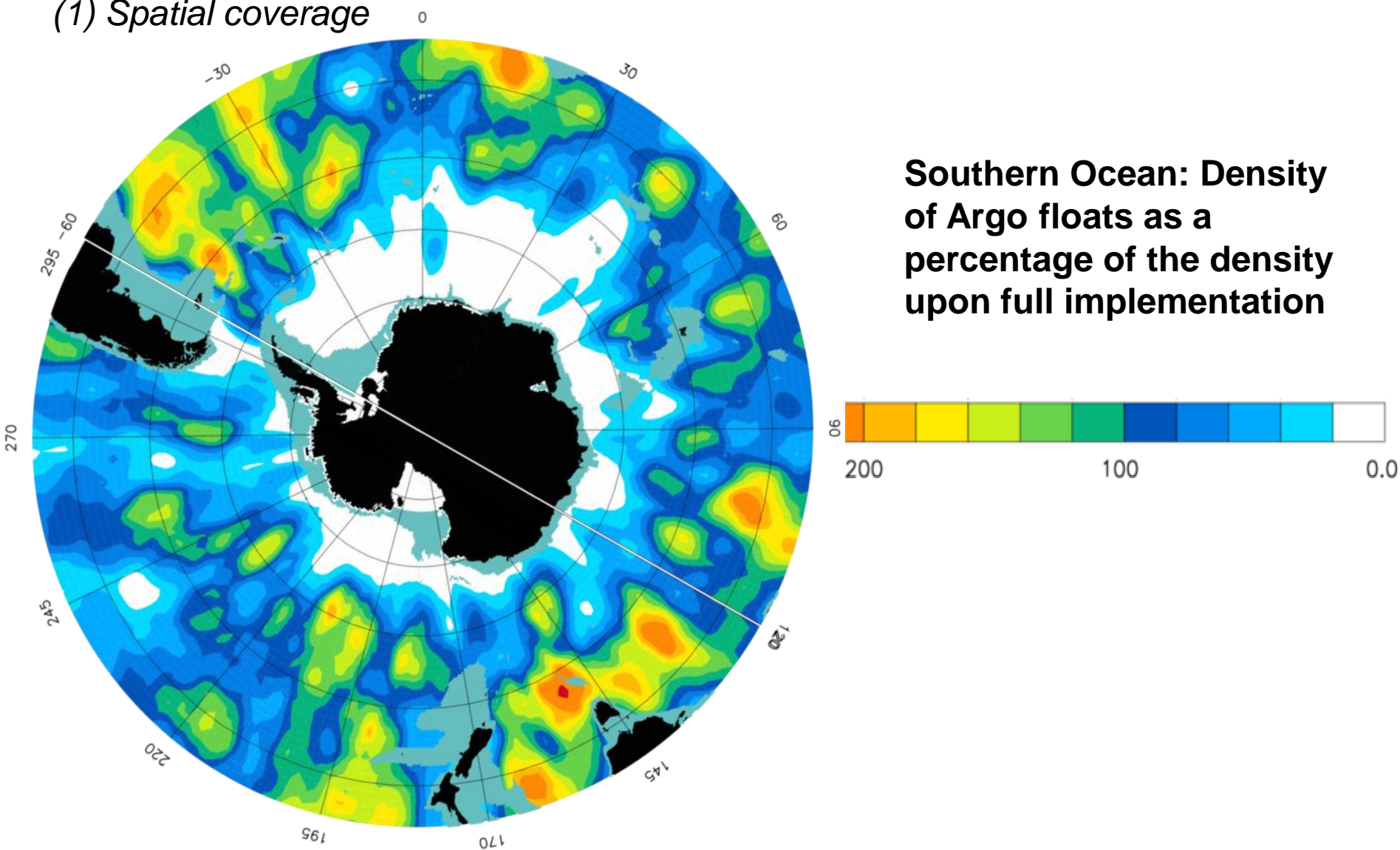


# **What are the most important remaining gaps?**

- 1. Spatial Coverage**
- 2. Proper specification of prior observation uncertainty for under-ice observations**

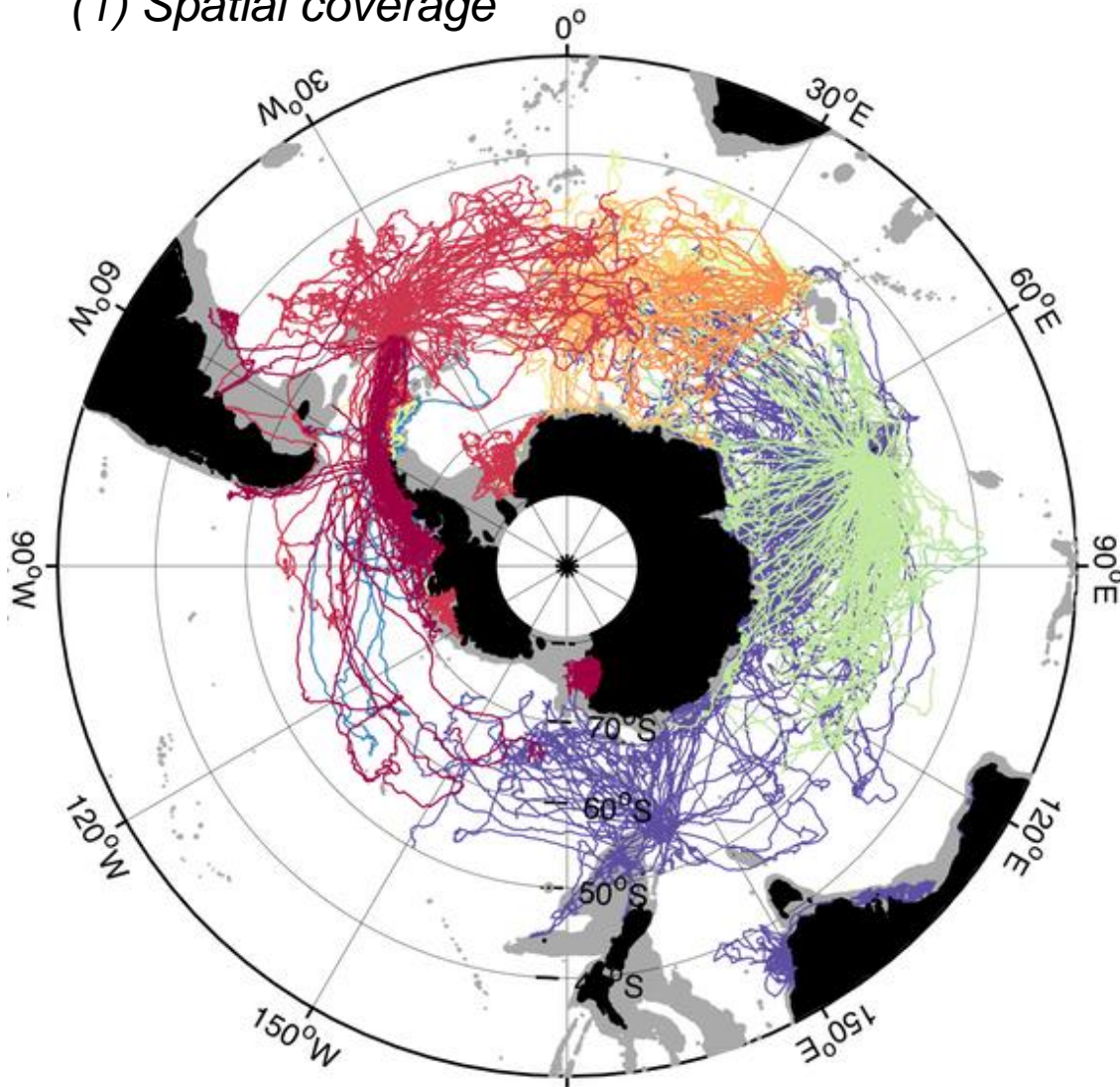
# What are the most important remaining gaps?

(1) *Spatial coverage*



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(1) *Spatial coverage*



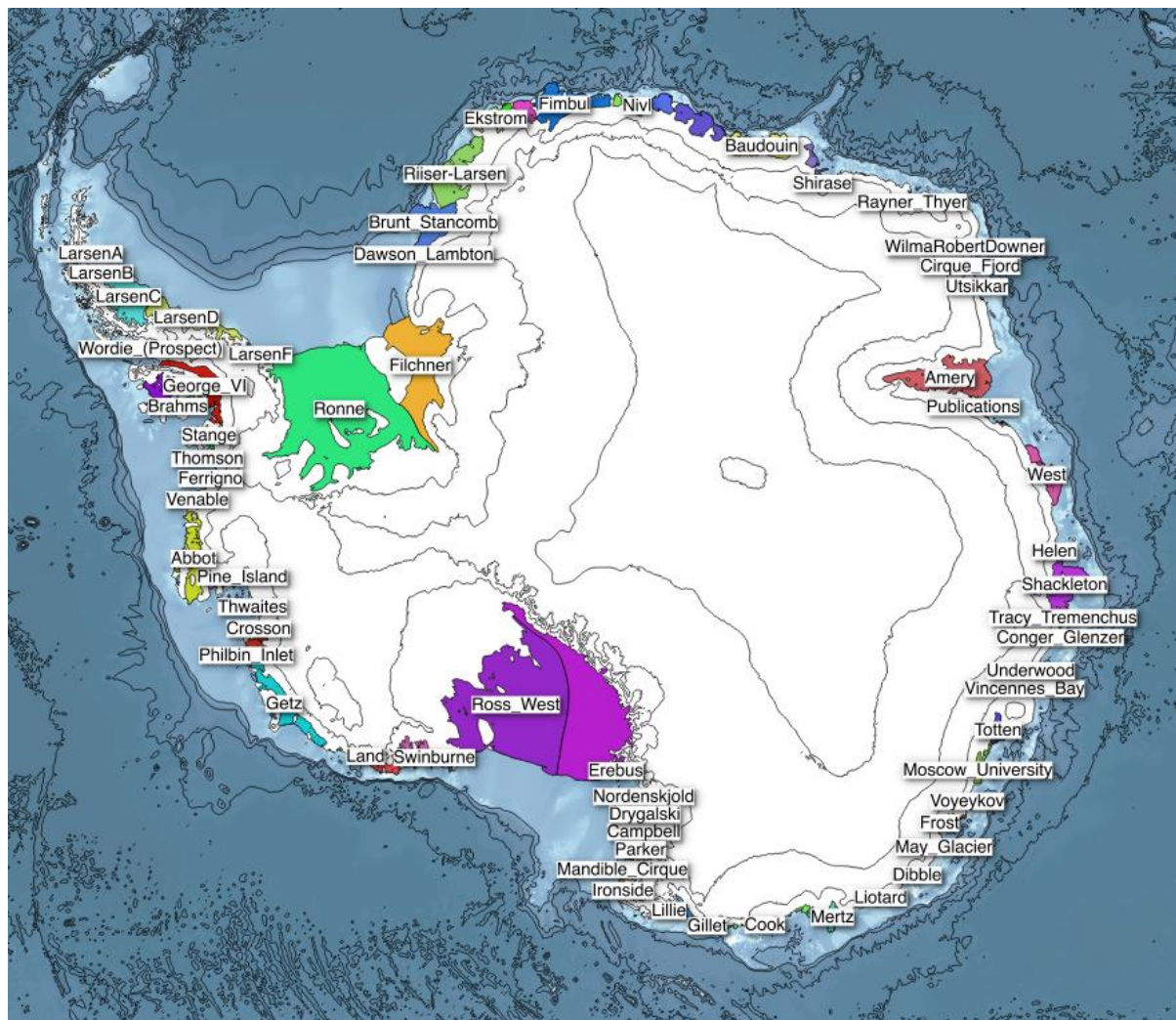
**MEOP CTD database**





# What are the most important remaining gaps?

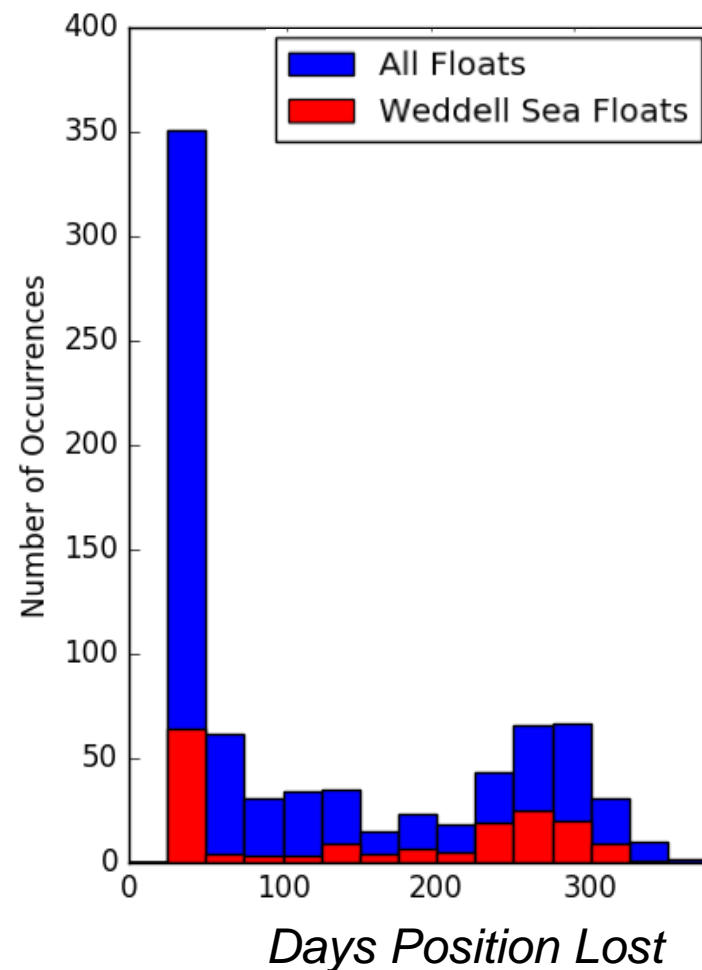
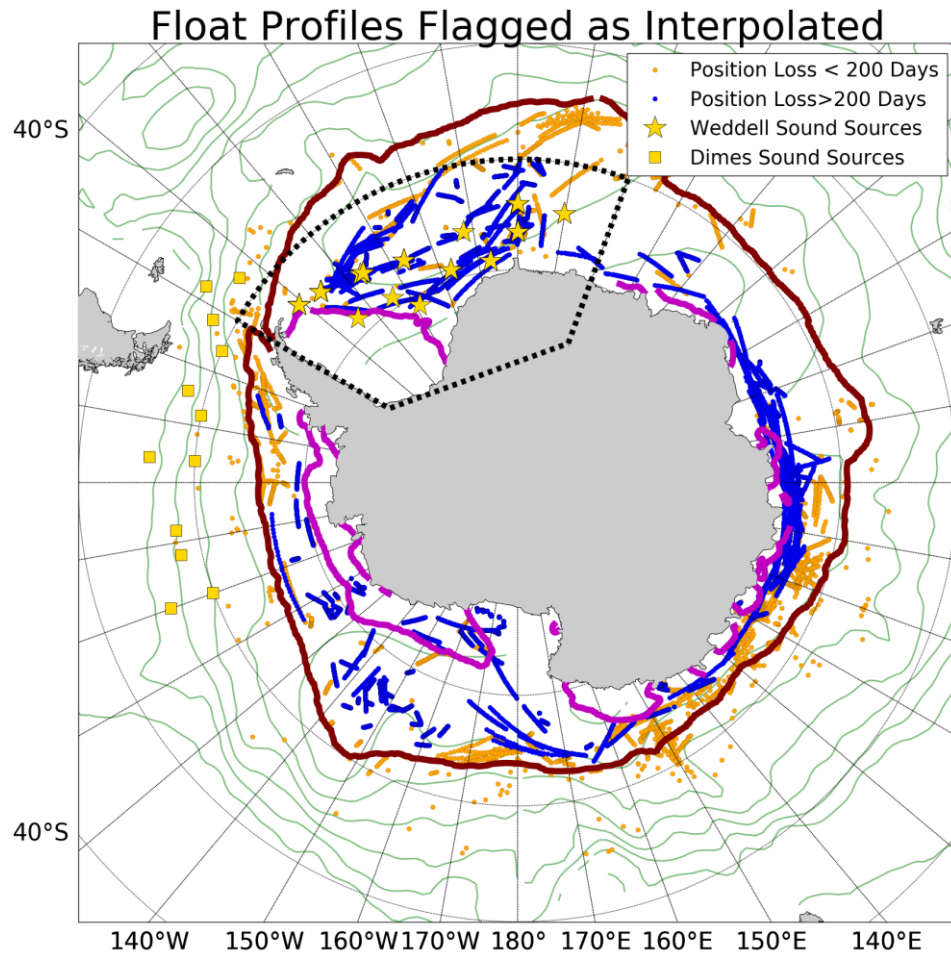
## (1) Spatial coverage





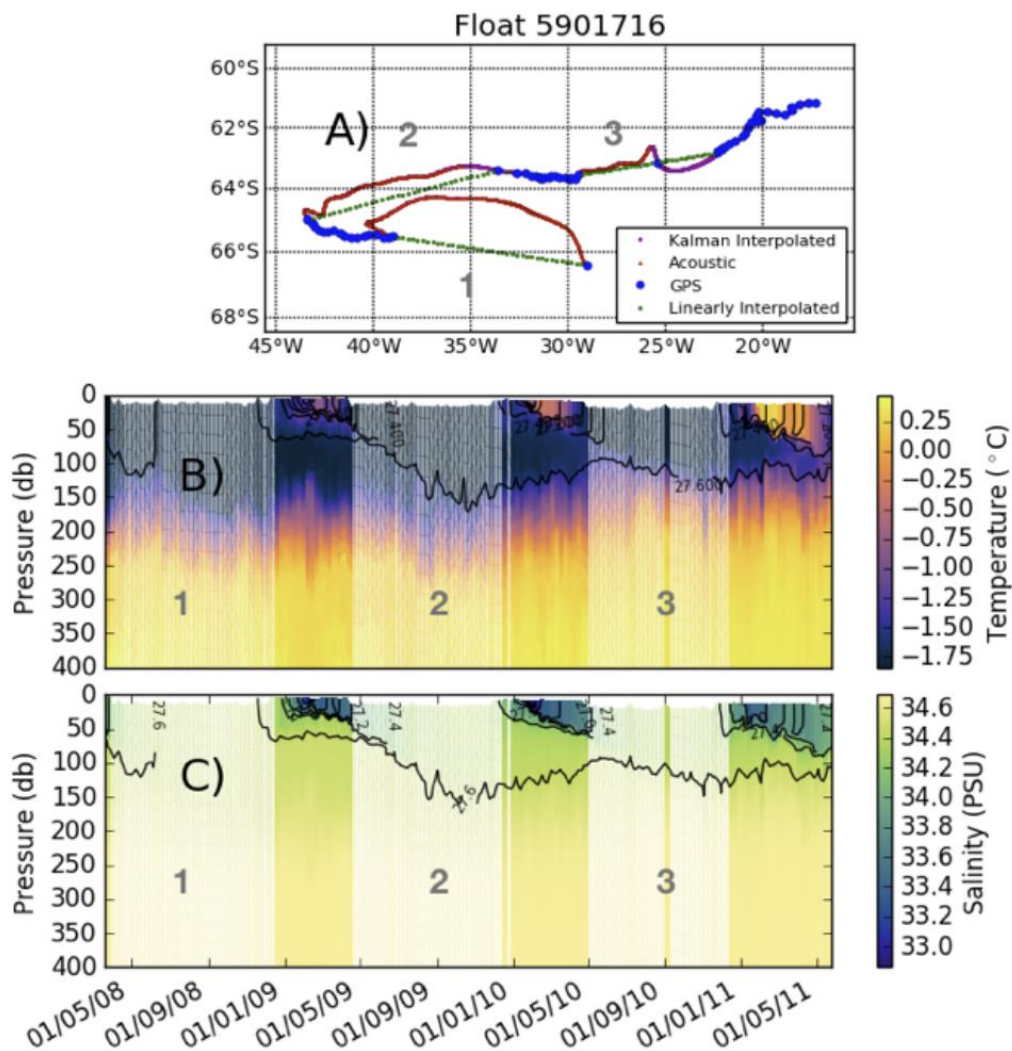
# What are the most important remaining gaps?

(2) *Proper specification of prior uncertainty for under-ice observations*



# What are the most important remaining gaps?

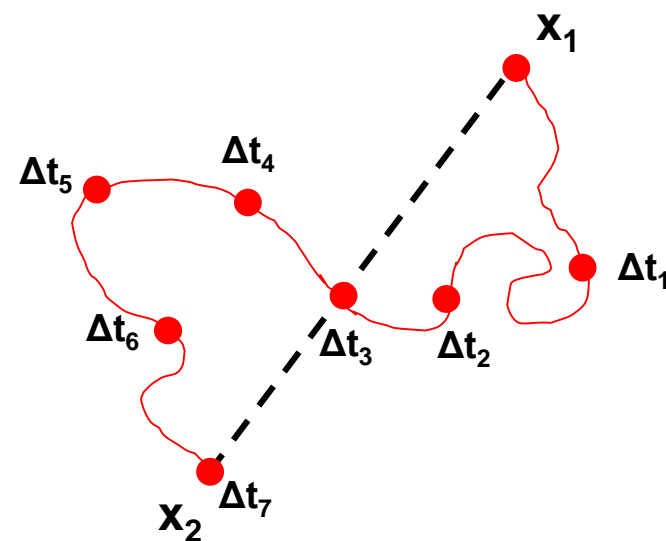
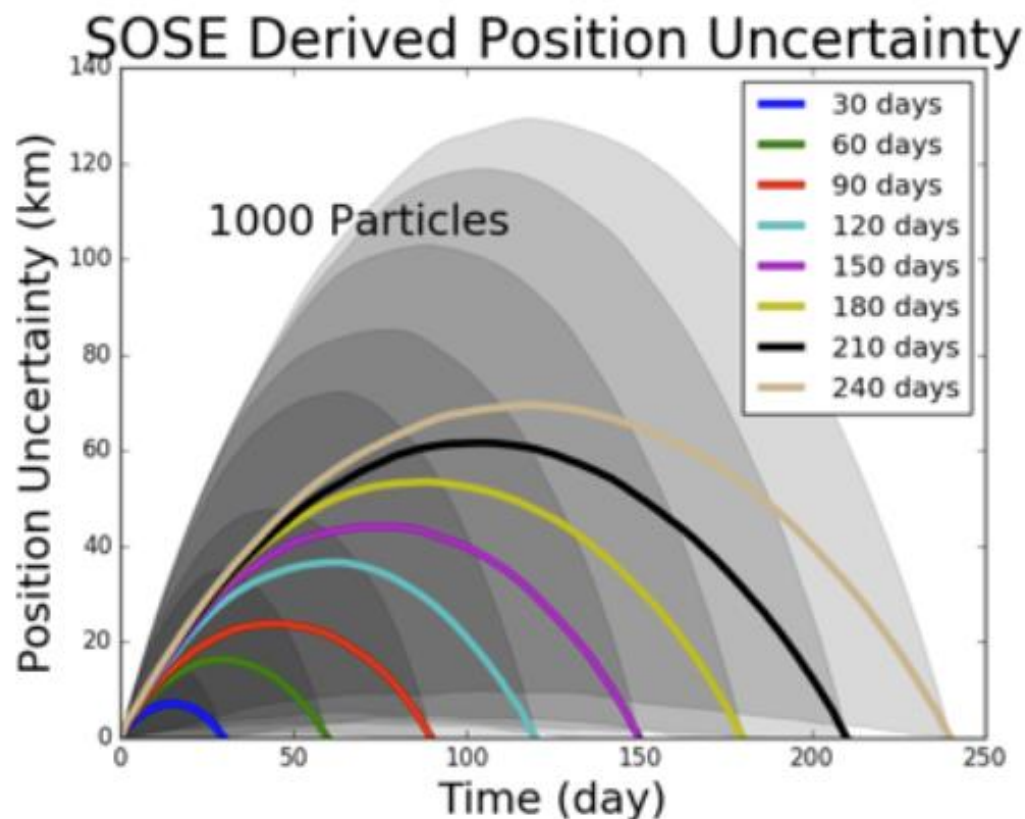
(2) *Proper specification of prior uncertainty for under-ice observations*



# What are the most important remaining gaps?

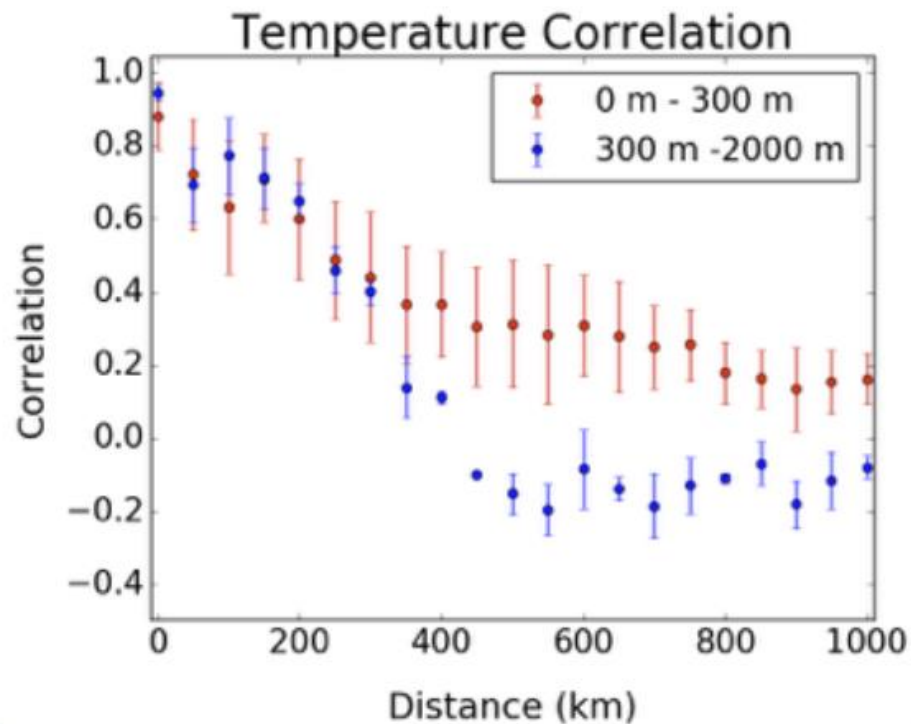
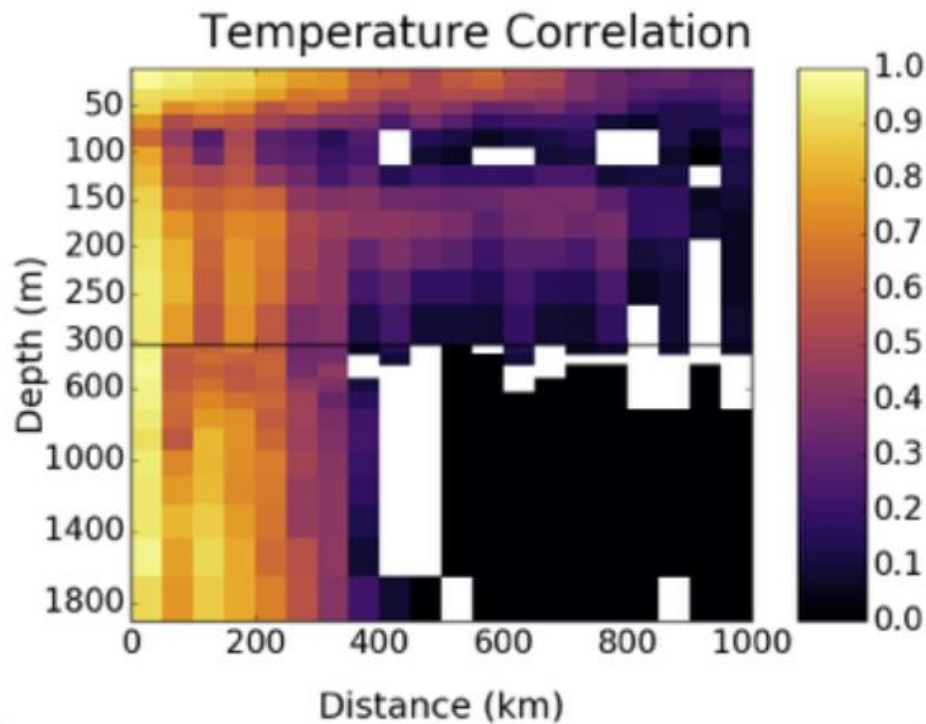
(2) *Proper specification of prior uncertainty for under-ice observations*

$$\sigma_{total}^2 = \sigma_{sensor}^2 + \sigma_{location}^2(x_1, x_2, \Delta t)$$



# What are the most important remaining gaps?

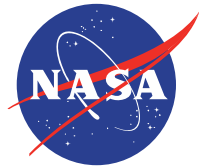
(2) *Proper specification of prior uncertainty for under-ice observations*



# Summary

- The synthesis of in situ T and S observations from Argo and Arctic ice-tethered profiles significantly improves ECCO ocean-ice state estimates.
- Large observational gaps remain in both the Arctic and Southern oceans, especially beneath ice shelves.
- The proper utilization of T and S profiles from floats that survive beneath sea ice for long periods of time requires careful thinking about how to specify their corresponding prior uncertainties as a function of time and space.
- Colleagues at Scripps are currently pursuing this important problem with promising results thus far.





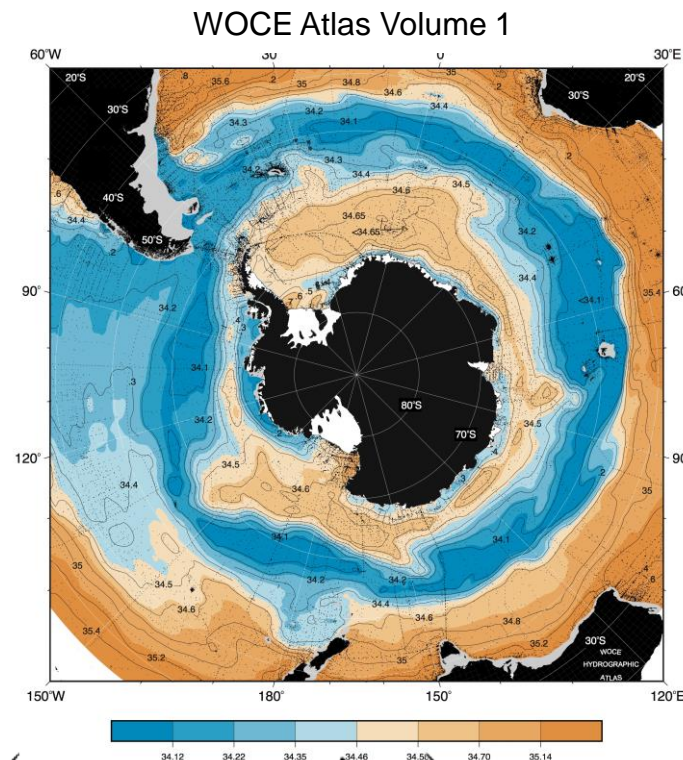
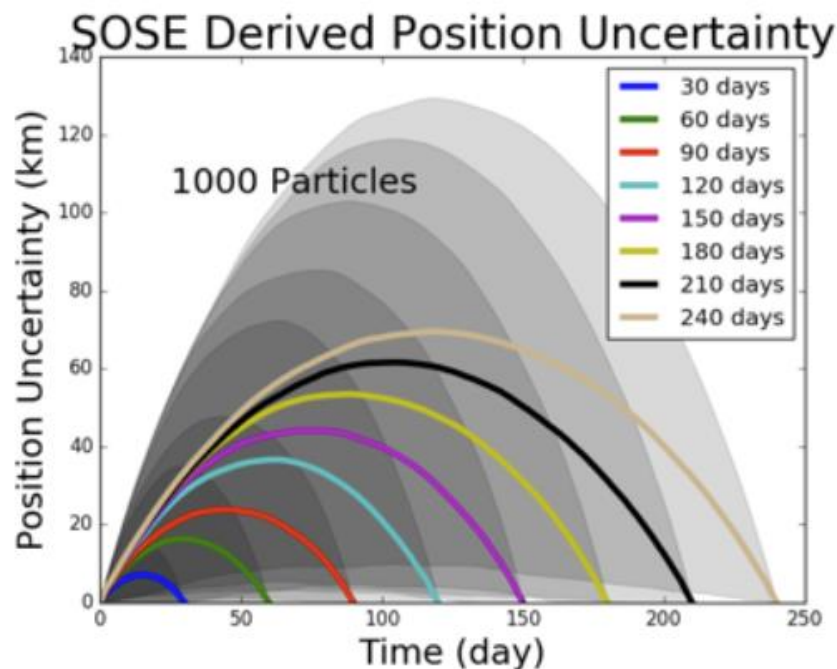
**Jet Propulsion Laboratory**  
California Institute of Technology

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[jpl.nasa.gov](http://jpl.nasa.gov)

# What are the most important remaining gaps?

(2) *Proper specification of prior uncertainty for under-ice observations*



$$\sigma_{total}^2 = \sigma_{sensor}^2 + \sigma_{location}^2(x_1, x_2, \Delta t)$$